

SM3 1.1 NH: Factoring with Two Terms

GCF: Factor out the greatest common factor only. If the lead coefficient is negative, factor it out.

$$1) \quad 9v^2 + 21v \\ 3v(3v + 7)$$

$$2) \quad 27m^5 + 18m^3 + 12m^2 + 6m \\ 3m(9m^4 + 6m^2 + 4m + 2)$$

$$3) \quad 30y^4x^2 + 21y^5 \\ 3y^4(10x^2 + 7y)$$

$$4) \quad 6x^2 - 24x + 30y - 6 \\ 6(x^2 - 4x + 5y - 1)$$

$$5) \quad 2b^5 + 5b - 5 \\ \text{prime}$$

$$6) \quad 16xz^2y^4 - 2x^2z^2 - 20xz^2 \\ 2xz^2(8y^4 - x - 10)$$

$$7) \quad -36y^2 - 6xy + 6 \\ -6(6y^2 + xy - 1)$$

$$8) \quad -42n^4 + 54n - 54n^2 \\ -6n(7n^3 - 9 + 9n)$$

Difference of Squares: Factor each polynomial completely over the integers.

$$9) \quad x^2 - 25 \\ (x + 5)(x - 5)$$

$$10) \quad 9n^2 - 4 \\ (3n + 2)(3n - 2)$$

$$11) \quad 8v^2 - 50 \\ 2(2v + 5)(2v - 5)$$

$$12) \quad 25n^2 - 4 \\ (5n + 2)(5n - 2)$$

$$13) \quad 5a^2 - 5 \\ 5(a + 1)(a - 1)$$

$$14) \quad 25k^2 - 9 \\ (5k + 3)(5k - 3)$$

$$15) \quad 3r^2 - 27 \\ 3(r + 3)(r - 3)$$

$$16) \quad 48n^2 - 75 \\ 3(4n + 5)(4n - 5)$$

$$17) \quad 4 - x^2 \\ (2 + x)(2 - x) \text{ or} \\ -(x + 2)(x - 2)$$

$$18) \quad 16 - 25m^2 \\ (4 + 5m)(4 - 5m) \text{ or} \\ -(5m + 4)(5m - 4)$$

$$19) \quad -32n^2 + 18 \\ -2(4n + 3)(4n - 3)$$

$$20) \quad -3k^2 + 48 \\ -3(k + 4)(k - 4)$$

$$21) 9x^2 + 4$$

prime

$$22) 5x^2 + 5$$
$$5(x^2 + 1)$$

$$23) 36x^2 - 100$$
$$4(3x + 5)(3x - 5)$$

$$24) 9a^2 - 1$$
$$(3a + 1)(3a - 1)$$

$$25) x^2 - 4y^2$$
$$(x + 2y)(x - 2y)$$

$$26) 9u^2 - v^2$$
$$(3u + v)(3u - v)$$

$$27) 45x^2 - 5y^2$$
$$5(3x + y)(3x - y)$$

$$28) 81m^2 - 36n^2$$
$$9(3m + 2n)(3m - 2n)$$

$$29) x^4 - 4$$
$$(x^2 + 2)(x^2 - 2)$$

$$30) y^4 - 16$$
$$(y^2 + 4)(y + 2)(y - 2)$$

$$31) 27x^4 - 75$$
$$3(3x^2 + 5)(3x^2 - 5)$$

$$32) 2p^4 - 32$$
$$2(p^2 + 4)(p + 2)(p - 2)$$

$$33) x^6 - 4$$
$$(x^3 + 2)(x^3 - 2)$$

$$34) x^6 - 25$$
$$(x^3 + 5)(x^3 - 5)$$

$$35) 25n^6 - 1$$
$$(5n^3 + 1)(5n^3 - 1)$$

$$36) 2n^6 - 18$$
$$2(n^3 + 3)(n^3 - 3)$$

Sum or Difference of Cubes: Factor each polynomial completely over the integers.

$$37) x^3 - 64$$
$$(x - 4)(x^2 + 4x + 16)$$

$$38) a^3 + 1$$
$$(a + 1)(a^2 - a + 1)$$

$$39) u^3 - 64$$
$$(u - 4)(u^2 + 4u + 16)$$

$$40) 2a^3 + 2$$
$$2(a + 1)(a^2 - a + 1)$$

$$41) 4 - 108x^3$$
$$-4(3x - 1)(9x^2 + 3x + 1)$$

$$42) 16x^3 - 54$$
$$2(2x - 3)(4x^2 + 6x + 9)$$

$$43) 3m^3 + 648 \\ 3(m + 6)(m^2 - 6m + 36)$$

$$44) x^3 - 125 \\ (x - 5)(x^2 + 5x + 25)$$

$$45) y^3 + 216 \\ (y + 6)(y^2 - 6y + 36)$$

$$46) 1 + 27x^3 \\ (1 + 3x)(1 - 3x + 9x^2) \text{ or} \\ (3x + 1)(9x^2 - 3x + 1)$$

$$47) -8x^3 + 1 \\ -(2x - 1)(4x^2 + 2x + 1)$$

$$48) -375m^3 + 192 \\ -3(5m - 4)(25m^2 + 20m + 16)$$

$$49) 125x^3 + y^3 \\ (5x + y)(25x^2 - 5xy + y^2)$$

$$50) 648x^3 - 3y^3 \\ 3(6x - y)(36x^2 + 6xy + y^2)$$

$$51) 125x^6 + 27 \\ (5x^2 + 3)(25x^4 - 15x^2 + 9)$$

$$52) 250x^6 - 16 \\ 2(5x^2 - 2)(25x^4 + 10x^2 + 4)$$

$$53) -125x^6 + 216 \\ -(5x^2 - 6)(25x^4 + 30x^2 + 36)$$

$$54) 81x^6 - 3 \\ 3(3x^2 - 1)(9x^4 + 3x^2 + 1)$$

$$55) x^6 - 279 \\ \text{prime}$$

$$56) 729x^6 - 64 \\ (3x + 2)(3x - 2)(81x^4 + 36x^2 + 16)$$

57) Challenge: Factor completely over the integers.

$$x^6 - 1$$

$$(x + 1)(x^2 - x + 1)(x - 1)(x^2 + x + 1)$$